





NATIONAL LEVEL SCIENCE TALENT SEARCH EXAMINATION (UPDATED)

CLASS - 9

Question Paper Code : UN489

KEY

1. B	2. B	3. C	4. A	5. C	6. D	7. D	8. A	9. B	10. D
11. C	12. A	13. B	14. C	15. C	16. B	17. D	18. C	19. D	20. A
21. C	22. D	23. B	24. C	25. B	26. C	27. D	28. A	29. D	30. B
31. B	32. C	33. B	34. D	35. C	36. C	37. B	38. B	39. C	40. D
41. D	42. D	43. A	44. D	45. A	46. C	47. A	48. C	49. B	50. D
51. B	52. B	53. C	54. D	55. D	56. C	57. A	58. A	59. D	60. C

MATHEMATICS

SOLUTIONS

- 01. (B) Cost : Join EC
 - Area of $\triangle ABD = \frac{1}{3}$ of area of $\triangle ABC$ = 120 cm²



 \therefore Area of $\triangle ABE = Area of <math>\triangle ADE$

$$=\frac{1}{2}\times 120 \text{ cm}^2 = 60 \text{ cm}^2$$

In \triangle BCD, CE is median \Rightarrow Area of \triangle BCD

 \therefore Area of \triangle CDE = Area of \triangle BCE

$$=\frac{1}{2}\times 240 \text{ cm}^2 = 120 \text{ cm}^2$$

 $\therefore \qquad \frac{\mathsf{EF}}{\mathsf{EA}} = \frac{\mathsf{Area of } \Delta \mathsf{BEF}}{\mathsf{Area of } \Delta \mathsf{ABE}} = \frac{\mathsf{Area of } \Delta \mathsf{CEF}}{\mathsf{Area of } \Delta \mathsf{ACE}}$

$$\Rightarrow \frac{x}{60} = \frac{120 - x}{(60 + 120)} \Rightarrow \frac{x}{60} \times 180^3 = 120 - x$$
$$4x = 120$$

Area of $\triangle BEF(x) = 30 \text{ cm}^2$

02. (B) In
$$\triangle ABC$$
, $\angle ABC = 180^\circ - 125^\circ = 55^\circ$
A
A
 $25^\circ 55^\circ 55^\circ c$
 $x \rightarrow D$
 $\therefore \angle ABC = \angle ACB = 55^\circ$
[\therefore Given in $\triangle ABC$, $AB = AC$]
In $\triangle ACD$, $\angle ACB = x + 25^\circ$
 $\therefore x + 25^\circ = 55^\circ$
 $x = 55^\circ - 25^\circ = 30^\circ$

03. (C)

$$\begin{array}{c|c|c} x - \sqrt{2} & x^{3} - 2\sqrt{2} & (x^{2} + \sqrt{2}x + 2) \\ \hline x^{3} - \sqrt{2}x^{2} \\ (-) & (+) & \\ \hline \sqrt{2}x^{2} - 2\sqrt{2} & \\ \sqrt{2}x^{2} - 2x & \\ (-) & (+) & \\ \hline 2x - 2\sqrt{2} & \\ 2x - 2\sqrt{2} & \\ (-) & (+) & \\ \hline 0 & \\ \end{array}$$

 $\frac{x^3 - 2\sqrt{2}}{x - \sqrt{2}} = \frac{x^3 - (\sqrt{2})^3}{x - \sqrt{2}} = \frac{(x - \sqrt{2})[x^2 + \sqrt{2}x + (\sqrt{2})^2]}{(x - \sqrt{2})}$ 04. (A) $\sqrt{10 + \sqrt{24} - \sqrt{60} - \sqrt{40}}$ $=\sqrt{10+2\sqrt{6}-2\sqrt{15}-2\sqrt{10}}$ $=\sqrt{10+2\sqrt{2}\times\sqrt{3}-2\sqrt{3}\times\sqrt{5}-2\sqrt{5}\times\sqrt{2}}$ $=\sqrt{(\sqrt{2})^{2} + (\sqrt{3})^{2} + (\sqrt{5})^{2} + 2\sqrt{2} \times \sqrt{3} - 2\sqrt{5} \times \sqrt{3} - 2\sqrt{3} \times \sqrt{2}}$ $=\sqrt{\left(\sqrt{2}+\sqrt{3}-\sqrt{5}\right)^2}$ $=(\sqrt{2}+\sqrt{3}-\sqrt{5})$

(OR)

05. (C) Given
$$p(x) = \frac{2x+1}{x-2}$$

$$\therefore \quad p\left(\frac{2x+1}{x-2}\right) = \frac{2\left(\frac{2x+1}{x-2}\right)+1}{\left(\frac{2x+1}{x-2}\right)-2}$$

$$= \frac{\left[\frac{4x+2+(x-2)}{x-2}\right]}{\left[\frac{2x+1-2(x-2)}{x-2}\right]}$$

$$= \frac{(4x+2+x-2)}{(x-2)} \times \frac{(x-2)}{(2x+1-2x+4)}$$

$$= \frac{5x}{5} = x$$

06. (D) Proudct of two irrational numbers is a real number.

07. (D)
$$\frac{1}{\sqrt{11}-3} = \frac{1}{\sqrt{11}-3} \times \frac{\sqrt{11}+3}{\sqrt{11}+3}$$
$$= \frac{\sqrt{11}+3}{(\sqrt{11})^2 - 3^2} = \frac{\sqrt{11}+3}{11-9} = \frac{\sqrt{11}+3}{2}$$

Similarly,

$$\frac{1}{3-\sqrt{7}} = \frac{3+\sqrt{7}}{2}$$
$$\frac{1}{\sqrt{7}-\sqrt{5}} = \frac{\sqrt{7}+\sqrt{5}}{2}$$
$$\frac{1}{\sqrt{5}-\sqrt{3}} = \frac{\sqrt{5}+\sqrt{3}}{2}$$
$$\therefore \quad \frac{\sqrt{5}+\sqrt{3}}{2} < \frac{\sqrt{7}+\sqrt{5}}{2} < \frac{3+\sqrt{7}}{2} < \frac{\sqrt{11}+3}{2}$$
i.e.,
$$\frac{1}{\sqrt{5}-\sqrt{3}} < \frac{1}{\sqrt{7}-\sqrt{5}} < \frac{1}{3-\sqrt{7}} < \frac{1}{\sqrt{11}-3}$$
$$\Rightarrow \quad \sqrt{5}-\sqrt{3} > \sqrt{7}-\sqrt{5} > 3-\sqrt{7} > \sqrt{11}-3$$



32 cm R 41cm 41cm 32 cm С 9 m Construction : AE \perp CD and BF \perp CD $\Delta ADE \cong \Delta BCF [\because RHS congruency]$ $DE = FC [\because CPCT]$ But ABFE is a rectangle EF = AB = 32 cm:. DE = CF = $\frac{50 \text{ cm} - 32 \text{ cm}}{2} = 9 \text{ cm}$ In $\triangle ADE$, LE = 90° $\Rightarrow AD^2 = AE^2 + ED^2$ $41^2 = 9^2 + AE^2$ $41^2 - 9^2 = AE^2$ $(41 + 9)(41 - 9) = AE^2$ $50 \times 32 = AE^2$ $\sqrt{1600} = AE$ AE = 40 cmArea of the trapezium ABCD $=\frac{1}{2} \times AE(AB+CD)$ $=\frac{1}{2} \times 40^{20} (32+50) \text{ cm}^2$ = 1640 cm² Extend the line DC to a point P, such that AB||CP, 85° C Then $\angle BCP = \angle EDC = x^{\circ}$ (Corresponding angles) Also, $\angle ABC + \angle BCP = 180^{\circ}$ $\angle BCP = 95^{\circ}$ and $\angle BCP = \angle EDC = 95^{\circ}$

12. (A) Given
$$3\pi r^2 = 1848 \text{ cm}^2$$

$$\Rightarrow 3 \times \frac{22}{7} \times r^2 = 1848 \text{ cm}^2$$

$$r^2 = \frac{28}{4646} \times \frac{7}{22} \times \frac{1}{3} \text{ cm}^2$$

$$r = \sqrt{196} = 14 \text{ cm}$$
Volume of hemisphere
$$= \frac{2}{3} \times \pi \times 14 \times 14 \times 14 \text{ cm}^3$$
Given
$$\frac{1}{3} \pi \times 7 \times 7 \times h = \frac{2}{3} \times \pi \times 14 \times 14 \times 14$$

$$h = \frac{2}{3} \times 14^2 \times 14 \times 3 \times \frac{1}{3} \times$$

$$\Rightarrow (x^{2})^{3} + 3x^{2} \times \frac{1}{x^{2}} \left(x^{2} + \frac{1}{x^{2}} \right) + \left(\frac{1}{x^{2}} \right)^{3} = 27$$

$$\Rightarrow x^{6} + 3(3) + \frac{1}{x^{6}} = 27$$

$$\Rightarrow x^{6} + \frac{1}{x^{6}} = 27 - 9 = 18$$
14. (C) From the given figure, we have
AD = BC
$$\Rightarrow AD - CD = BC - CD$$
[Equal are subtracted from equals]
$$\Rightarrow AC = BD$$
15. (C) Const draw QT || RS
$$= \frac{0}{Q} + \frac{1}{Q} +$$

$$\therefore \quad \angle RQT = 180^{\circ} - 112^{\circ}$$
$$\angle RQT = 68^{\circ}$$
But $\angle OPQ = \angle PQT$
$$[\because Alternative angles]$$

$$\therefore \quad \angle OPQ = \angle PQR + \angle RQT$$
$$= 19^{\circ} + 68^{\circ} = 87^{\circ}$$

16. (B) LHS =
$$\frac{4(x+1)+5(x-1)+6}{x^2-1}$$

$$=\frac{4x+4+5x-5+6}{x^2-1}$$

$$=\left(\frac{9x+5}{x^2-1}\right)$$

17. (D)
$$\frac{15}{\sqrt{10} + \sqrt{20} + \sqrt{40} - \sqrt{5} - \sqrt{80}}$$
$$= \frac{15}{\sqrt{10} + 2\sqrt{5} + 2\sqrt{10} - \sqrt{5} - 4\sqrt{5}}$$
$$= \frac{15}{3\sqrt{10} - 3\sqrt{5}} = \frac{\frac{15}{45}}{\cancel{2}(\sqrt{10} - \sqrt{5})}$$
$$= \frac{5}{\sqrt{10} - \sqrt{5}} \times \frac{\sqrt{10} + \sqrt{5}}{\sqrt{10} + \sqrt{5}} = \frac{\cancel{5}(\sqrt{10} + \sqrt{5})}{\cancel{5}}$$

18. (C)
$$\frac{12.5}{\cancel{10} - \sqrt{5}} \times \frac{\sqrt{10} + \sqrt{5}}{7.5} = \frac{\cancel{5}(\sqrt{10} + \sqrt{5})}{\cancel{5}}$$
$$\frac{\cancel{5}(\sqrt{10} + \sqrt{5})}{\cancel{5}} = \frac{\cancel{5}(\sqrt{10} + \sqrt{5})}{\cancel{5}}$$
$$\frac{\cancel{5}(\sqrt{10} + \sqrt{5})}{\cancel{5}} = \frac{\cancel{5}(\sqrt{10} + \sqrt{5})}{\cancel{5}}$$
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$$\frac{\cancel{5}(\sqrt{10} - \sqrt{5})}{\cancel{5}} = \frac{\cancel{5}(\sqrt{10} + \sqrt{5})}{\cancel{5}}$$
$$\frac{\cancel{5}(\sqrt{10} + \sqrt{5})}{\cancel{5}} = \frac{\cancel{5}(\sqrt{10} + \sqrt{5})}{\cancel{5}} = \frac{\cancel{5}(\sqrt{10} + \sqrt{5})}{\cancel{5}}$$
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19. (D) 999999999 - 1 = (99,99,99,999)² - 1²
= (99,99,999999 + 1)(99,99,99,999 - 1)
= (1,00,00,00,000 × 99999998
= 99999998 × 10⁹
20. (A)
$$\frac{125x^3}{64} - \frac{75x^2}{8} + 15x - 8$$

 $= \left[\left(\frac{5x}{4} \right)^3 - 3 \times \frac{25}{16} x^2 \times 2 + 3 \times \frac{5}{4} x \times 4 - 2^3 \right]$
 $= \left[\left(\frac{5x}{4} \right)^3 - 3 \left(\frac{5x}{4} \right)^2 (2) + 3 \times \frac{5x}{4} \times 2^2 - 2^3 \right]$
 $= \left[\left(\frac{5x}{4} - 2 \right)^3 \right]$
 $= \left(\frac{5x}{4} - 2 \right)^2 \left(\frac{5x}{4} - 2 \right)$
 $= \left[\frac{25}{16} x^2 - \cancel{2} \times \frac{5}{\cancel{4}} \cancel{2} \times \cancel{2} + 2^2 \right] \left(\frac{5x}{4} - 2 \right)$
 $= \left(\frac{25x^2}{16} - 5x + 4 \right) \left(\frac{5x}{4} - 2 \right)$.
21. (C) On *y*-axis at the *x*-coordinates are zero
 \therefore 2(0) - 3*y* = 6
 $-3y = 6$
 $y = \frac{6}{-3} = -2$
 \therefore Required point = (0, -2)

24. (C) Side of each tile are 36 cm, 29 cm & 25 cm
∴
$$S = \frac{a+b+c}{2} = \frac{(36+29+25)}{2} cm$$

 $S = 45 cm$
Area of each tile
 $= \sqrt{S(s-a)(s-b)(s-c)}$
 $= \sqrt{45 \times 9 \times 16 \times 20} cm^2$
 $= \sqrt{5 \times 9 \times 9 \times 4 \times 4 \times 5 \times 2 \times 2} cm^2$
 $= 5 \times 9 \times 4 \times 2 cm^2$
 $= 360 cm^2$
∴ Area of 16 tiles = 360 cm² × 16
 $= 5760 cm^2$
∴ Total cost for polishing
 $= 5760 cm^2 \times \frac{80 \text{ paise}}{1 cm^2}$
 $= ₹ 576 / 9 \times \frac{8 / 9}{1 / 9 / 9}$
 $= ₹ 4608$
25. (B) Given $r = AC = 53 \& LB = 90^\circ$
∴ $AC^2 = AB^2 + BC^2$
 $53^2 - 45^2 = BC^2$
 $(53 + 45)(53 - 45) = BC^2$
 $98 \times = BC^2$
 $\sqrt{49 \times 16} = BC$
 $BC = 7 \times 4 = 28$
Area of the rectangle ABCD = AB × BC
 $= 45 \times 28 cm^2$
 $= 1260 cm^2$

PHYSICS

26.	(C)	The gravitational force that the moon				
		exerts on the planet is equal in				
		magnitude to the gravitational force that				
		the planet exerts on the moon (Newton's				
		third law).				

27. (D) As per Newton's 3rd law, the same force pulls both the trolleys. Let mass of X and Y be 2 m and m respectively.

Force on X is ma = Force on Y is ma.

 \therefore 2 m × 2 = m × a

So, a = 4 m/s² i.e., 4 m/s² is the initial acceleration of Y.

- 28. (A) The K.E is maximum at point Q. The total energy is the same at all the points.
- 29. (D) In the first case:

Initial velocity, u = 0

Final velocity, $v = 6 \text{ m s}^{-1}$

Time, t = 30 s

Acceleration a = $\frac{v-u}{t}$

Substituting the given values of u, v and t in the above equation, we get

$$a = \frac{(6 \text{ m s}^{-1} - 0 \text{ m s}^{-1})}{30 \text{ s}} = 0.2 \text{ m s}^{-2}$$

In the second case :

Initial velocity, u = 6 m s⁻¹

Final velocity, $v = 4 \text{ m s}^{-1}$

Time, t = 5 s

Then,
$$a = \frac{(4 \text{ m s}^{-1} - 6 \text{ m s}^{-1})}{5 \text{ s}} = -0.4 \text{ m s}^{-2}$$

The acceleration of the bicycle in the first case is 0.2 m s⁻² and in the second case, it is - 0.4 m s⁻².

30. (B) Due to inertia of motion, the water in the tank would move forward on sudden application of the brake.

31. (B)
$$\frac{1}{2}mv^2 = 1500$$

$$m = \frac{1500 \times 2}{10^2} = 30 \text{ kg}$$

$$X = \frac{1}{2}mv^2 = \frac{1}{2} \times 30 \times 40^2 = 24\ 000\ J$$

Increase in Kinetic energy

= 24 000 - 1500 = 22 500 J

32. (C) Distance travelled = Area under the speed-time graph. If the object is moving with constant speed, its speed-time graph must be a horizontal straight line.

Distance covered is equaled to the area under the straight line.

- 33. (B) Inertia is the property of mass that resists changes in motion. A body at rest tends to remain at rest.
- 34. (D) The principle of conservation of energy states that the total energy of a system remains constant. The total energy includes the internal energy. The total of KE and PE at the end is 0.
- 35. (C) Density of iron, d = 7.8×10^{-3} kg/m³ Volume of iron piece,

V = 100 cm³ = 100 × 10⁻⁶ m³ = 10⁻⁴ m³

Mass of iron piece,

 $M = V \times d = (10^{-4} \text{ m}^3) \times (7.8 \times 10^{-3} \text{ kg/m}^3)$ = 0.78 kg

Weight of iron piece,

W = Mg = (0.78 kg)(10 m/s²) = 7.8 N

(b) Upthrust, F_B = Weight of water displaced
 = Volume of water displaced × Density of water × g

= Volume of iron piece × density of water × g

(volume of water displaced = Volume of iron piece)

 $= (10^{-4} \text{ m}^3)(1000 \text{ kg/m}^3)(10 \text{ m/s}^2) = 1 \text{ N}$

(c) Apparent weight = true weight of iron piece – upthrust on iron piece in water

$$= W - F_{p} = 7.8 N - 1 N = 6.8 N.$$

CHEMISTRY

- 36. (C) Equal volumes contain equal no. of molecules. Hence, no. of atoms of H₂, He, O_2 and O_3 will be in the ratio 2:1:2:3.
- Mass of solute Mass% = -37. (B) Mass of solute + Solvent

(A) Mass% =
$$\frac{5}{5+95} \times 100 = 5$$

(B) Mass% =
$$\frac{15}{150} \times 100 = 10$$

(C) Mass% =
$$\frac{10}{200} \times 100 = 5$$

(D) Mass% =
$$\frac{25}{400} \times 100 = 6.25$$

15 g of oxalic acid present in 150 g of its aqueous solution has maximum mass percentage.

38. (B)

(i) Molecular mass of C₆H₅COOH $= 6 \times at.$ mass of C + 5 $\times at.$ mass of H + $1 \times at.$ mass of C + at. mass of O + at. mass of O + at. mass of H $= 6 \times 12.0 \text{ u} + 5 \times 1.0 \text{ u} + 1 \times 12.0 \text{ u} + 16 \text{ u}$ + 16 u + 1.0 u = 72 + 5 + 12 + 16 + 16 + 1 = 122 u(ii) Molecular mass of Al_2O_3 = 2 × at. mass of Al + 3 × at. mass of O $= 2 \times 27 u + 3 \times 16 u = 102 u$ Molecular mass of Na₂SO₄ (iii) = $2 \times at$. mass of Na + at. mass of S + $4 \times$ at. mass of O $= 2 \times 23 u + 32 u + 4 \times 16 u = 142 u.$ 39. (C) Statements I, II and VI are true. 40. (D) An ice cube and water have mass and occupy space, so they are matter. An ice cube has a definite shape and a

definite volume, so it is a solid.

Water has a definite volume but has no definite shape, so it is a liquid.

- 41. (D) With chlorine, phosphorus forms PCl_{2} and $\mathrm{PC}l_{\scriptscriptstyle \mathrm{S}}.$ NH_4^+ ion is a cation and is made up of N and H which are non-metal atoms.
- 42. (D) The solubility of a solid in water as solvent will increase if you increase the temperature of water.
- 43. (A)
 - (i) Molecular mass of C₁₂H₂₂O₁₁ = 12 × At. mass of C + 22 × At. mass of H + 11 × At. mass of O

= 12 × 12.0 u + 22 × 1.0 u + 11 × 16.0 u = 144 + 22 + 176 u = 342 u.

(ii) Molecular mass of $Al_{2}(SO_{4})$

> = 2 × At. mass of $Al + 3 \times [At. mass of S]$ + 4 × At. mass of O]

$$= 2 \times 27.0 \text{ u} + 3 \times (32.0 \text{ u} + 4 \times 16.0 \text{ u})$$

 $= 54 \text{ u} + 3 (32 + 64) \text{ u} = 54 + 3 \times 96 \text{ u} = 54$ + 288 u = 342 u.

Molecular mass of CuSO₄.5 H₂O (iii)

> = At. mass of Cu + At. mass of $S + 4 \times At$. mass of $O + 5 \times (2 \times At. mass of H + 1 \times$ At. mass of O)

= 63.5 + 32.0 + 64.0 + 90.0 u = 249.5 u.

- 44. (D) The solubility of NaCl remains the same i.e., = 35 °C at all temperatures.
- 45. (A) Lower the melting points of substances, weaker or lower are the interparticle forces of attraction.

Higher the melting points of substances, stronger or higher are the interparticle forces of attraction. The increasing order of four substances P, Q, R and S based on their interparticle forces of attraction is P(78 °C), R (100 °C), S (168 °C) and Q (262 °C).

BIOLOGY

- 46. (C) X-Granulocytes and Y-Agranulocytes.
- 47. (A) The longest animal cell is nerve cell.
- 48. (C) Leucoplasts are the colourless plastids which store starch/protein and lipids in them.
- 49. (B) Rhinoviruses causes common cold.
- 50. (D) The functions performed by ribosomes are:
 - (i) It helps in the synthesis of enzymes.
 - (ii) It helps in synthesis of protein molecules.
- 51. (B) The scientific name of an organism include genus and species.
- 52. (B) Dendrites receives impulses.
- 53. (C) Through crop rotation with leguminous crops, nitrogen can be replenished in soil naturally. The leguminous plants, like peas, beans, soybeans, peanuts, etc., have nitrogen-fixing bacteria in their root nodules. For example, the nitrogenfixing bacteria, viz., Rhizobium, fixes atmospheric nitrogen (N_2) into ammonium (NH_4^+) which is used by the plants.
- 54. (D) The steps involved in the carbon cycle are: Photosynthesis, respiration, and burning of fossil fuels.
- 55. (D) Afforestation, contour ploughing, and step farming prevents soil erosion.

CRITICAL THINKING

56. (C) Except option (C) rest all can be drawn without lifting the pen.



- 57. (A) The moon cannot support life because it does not have an atmosphere and is not goologically active.
- 58. (A) WTSXZY (The first three components attached are WTS)

59. (D)





60. (C) From I, we conclude that 1st, 8th, 15th, 22nd and 29th of June 2020 were Mondays.

So, the last Monday fell on 29th.

From II, we conclude that 30th June, 2010 was Tuesday. Thus, 29th June 2020 was the last Monday of the month.

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The End